

Parametric Study of Composite Steel-Concrete Beams with External Prestressing

Amer M. Ibrahim, Saad k. Mohaisen, Qusay W. Ahmed

Abstract— The main purpose of the present paper is to investigate the effect of several important parameters on the behavior of external prestressed composite steel-concrete beams. ANSYS computer program (version 12.0) has been used to analyze the three dimensional model. The nonlinear material and geometrical analysis based on Incremental-Iterative load method, is adopted. These parameters include effect of compressive strength of concrete, effective prestressing stress to ultimate stress ratio, effective height to center of prestressing cables ,effect of external prestressing technique , type of loading, tendon profile, degree of interaction , ratio of thickness to width of concrete slab , using unsymmetrical I-steel beams ,effect of number of stiffeners and effect Full and Partial Interaction.

Index Terms— ANSYS; Parametric study; Externally prestressed; Composite steel-concrete beams.

1 INTRODUCTION

Externally prestressed structures, initially developed for bridges, are now becoming popular in bridge construction and strengthening or rehabilitation of existing structures. Comparing with an internal prestressing system, an external prestressing system has some advantages, such as being simpler to construct and easier to inspect and maintain.

The external prestressing of the steel or composite beams is accomplished by means of high strength tendons anchored at the two ends of steel beam. The cable profile (straight or draped) is determined along the beam axis by a specific number of saddles at which the cable can slip. Externally prestressing of steel structures or composite beams may be considered as a powerful economical alternative for strengthening the existing beams as well as for designing new beams.

Composite beams strengthened with prestressed tendons display several failure modes. These failure modes include (i) compression crushing of concrete (ii) yielding of steel beam web, (iii) shear failure, (iv) rupture of steel tendons. Out of these four failure modes, the fourth mode can be eliminated by providing special steel anchorages at the ends of and steel deviators along the tendons to eliminate stress concentrations. Shear failure can be prevented by providing sufficient shear studs on the steel beam, to be encased in concrete. The other two failure modes, namely, compression crushing of concrete and yielding of steel beam is considered the imported factors in composite steel-concrete beams failure.

There are many achievements for the prestressing technique concerning both experimental and analytical can be found. Li et al. [1] investigated the fatigue behavior of composite steel-concrete bridges by strengthening bridges with ex-

ternal tendons. They carried out parametric studies of the fatigue test for various components such as strands, shear studs, and cover plates and discussed the results by comparing them with the current bridge design specifications. Similarly, Dall'Asta and Zona [2] proposed a nonlinear finite element model simulating the behavior of beam tested by Ayyub et al. [7] to describe the structural behavior up to failure only ,while in this paper we will discuss the effect of ten parameters on the behavior of prestressed composite beam, also Dall'Asta and Zona used numerical equation procedure to analysis the model ,while we used a computer program (ANSYS) . Nie et al. [3] tested eight specimens considering different parameters .The slip effect between the steel and concrete interface and the increase of the prestressing tendon force with the increase of loading were accounted. Choi et al. [4] illustrated a systematic procedure of external post-tensioning technique for strengthening or rehabilitation of steel-concrete composite bridges based on the principle of virtual work. Xue et al. [5] investigated the Long-term behavior, the combined effects of creep and shrinkage of concrete and relaxation of prestressing tendons were considered. Recently, Zona et al. [6] introduced a new simplified method for evaluating the tendon traction increment at collapse and consequently the beam flexural strength without requiring a nonlinear analysis of the whole beam-tendon structural system. The method is based on the observation that the shapes of the axial strain and curvature distributions at collapse.

In this paper a finite element method using ANSYS computer program is used to investigate the effect of several important parameters on the behavior of prestressed composite steel-concrete beams. The simply supported composite steel-concrete beam tested by Ayyub et al. [7] has been selected to carry out the parametric study.

2 GENERAL DESCRIPTION OF ANALYZED BEAM

The beam is simply supported composite steel-concrete prestressed with external tendon and tested under positive bending moment by Ayyub et al. [7] As shown in Fig.1 , the beam is consisted of a concrete slab, a steel beam, and two prestressing tendons. The steel beam had a total length of 4.83 m and was

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- Amer M. Ibrahim. Professor, Civil engineering, Diyala university, Iraq, E-mail: amereng05@yahoo.com
 - Saad k. Mohaisen Asst. prof., Civil engineering, Al-Mustansiriya University, Iraq, E-mail: amereng05@yahoo.com
 - Qusay W. Ahmed, Asst. lecturer, Civil engineering, Diyala university, Iraq, E-mail: msc.qussay@yahoo.com

In this study, the ANSYS computer program was used for analyzing the prestressed composite steel-concrete beam with external tendon. A three dimensional element was used to representation the structure. Three-dimensional brick element with 8 nodes is used to model the concrete slab (SOLID65 in ANSYS) [8] . The element is defined by eight nodes having three degrees of freedom at each node: translations of the nodes in x, y, and z-directions. The concrete is assumed to be homogeneous and initially isotropic. The compressive uniaxial stress-strain relationship for concrete model is obtained by using the following equations to compute the multi-linear isotropic stress-strain curve for the concrete [9] as shown in Fig.2.

The models that have been considered have a number of parameters for each used element from element library in ANSYS for analogue representation of the tested beam; these parameters are summarized in Table 1.

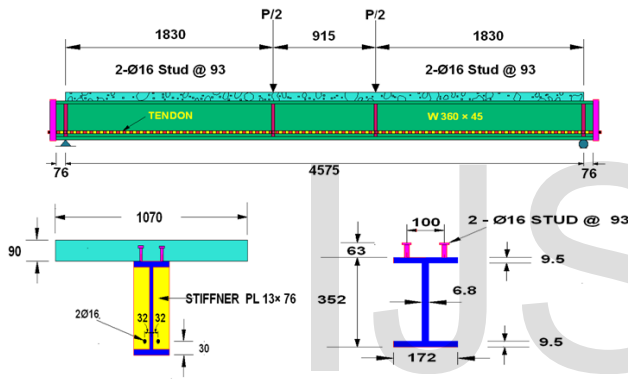


TABLE 1
Model Parameters for Used Elements in F.E. Model
(Units in Mpa)

	Concrete	Steel beam	Pre-stressing tendon
Ultimate compressive strength (MPa)	40		
Ultimate tensile strength (MPa)	4		
Young's modulus of elasticity (MPa)	29725	200000	200000
Poisson's ratio	0.2	0.3	
Yield strength (MPa)		411.6	915
Steel hardening (MPa)		6000	6000
Ultimate stress (MPa)		565.4	1091

$$f_c = \varepsilon E_c \quad \text{for} \quad 0 \leq \varepsilon \leq \varepsilon_1 \quad (1)$$

$$f_c = \frac{\varepsilon E_c}{1 + \left(\frac{\varepsilon}{\varepsilon_0}\right)^2} \quad \text{for} \quad \varepsilon_1 \leq \varepsilon \leq \varepsilon_0 \quad (2)$$

$$f_c = f'_c \quad \text{for} \quad \varepsilon_o \leq \varepsilon \leq \varepsilon_{cu} \quad (3)$$

$$\varepsilon_1 = \frac{0.3 f'_c}{E_c} \quad (\text{Hooke's law}) \quad (4)$$

$$\varepsilon_0 = \frac{2f_c'}{E_r} \quad (5)$$

web along the full length of the beam.

$$f_c = \varepsilon E_c \quad \text{for} \quad 0 \leq \varepsilon \leq \varepsilon_1 \quad (1)$$

$$f_c = \frac{\varepsilon E_c}{1 + \left(\frac{\varepsilon}{\varepsilon_0}\right)^2} \quad \text{for} \quad \varepsilon_1 \leq \varepsilon \leq \varepsilon_0 \quad (2)$$

$$f_c = f'_c \quad \text{for} \quad \varepsilon_o \leq \varepsilon \leq \varepsilon_{cu} \quad (3)$$

$$\varepsilon_1 = \frac{0.3 f_c'}{E_c} \quad (\text{Hooke's law}) \quad (4)$$

$$\mathcal{E}_0 = \frac{2 f_c'}{E_c} \quad (5)$$

where

ϵ_1 = strain corresponding to (0.3fc'). ϵ_o = strain at peak point.
 ϵ_{cu} = ultimate compressive strain.

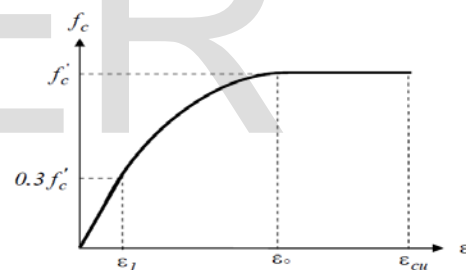


Fig. 2. Simplified Compressive Uniaxial Stress-Strain Curve for Concrete .

To represent the steel beam in finite element, three-dimensional 4-node shell element (SHELL43 in ANSYS) is used. The element has six degrees of freedom at each node: translations in the nodal x, y, and z directions and rotations about the nodal x, y, and z axes. In contrast to concrete, the mechanical properties of steel are well known, and it is a much simpler material to be represented. The strain-stress behavior can be assumed to be identical in tension and compression. To avoid possible computational difficulties when using a computer, the alternative bilinear stress-strain relationship indicated in Fig.3 is used [11].

In the present work, the strain hardening modulus (E_t) is assumed to be $(0.03 E_s)$. This value is selected to avoid convergence problems during iteration.

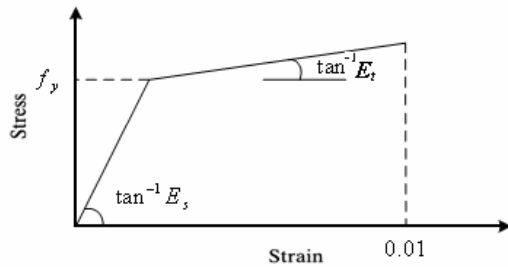


Fig. 3 Bilinear Stress-Strain Relationship for steel

For reinforcement and prestressing bars modeling since the ordinary steel bars and prestressing cable are slender, they can be assumed to transmit axial force only. Modeling of ordinary steel and prestressed steel in finite element is much simpler. The stress-strain relationship for ordinary reinforcing steel and prestressing tendons can be represented as shown in Fig. 3.

A three-dimensional nonlinear surface-to-surface "contact-pair" element was used to model the nonlinear behavior of the contact surface between concrete slab and steel beam. (CONTA-173 in ANSYS) and the other represents rigid surface taken as a target surface (TARGE-170 in ANSYS) [10]. In the present work, coefficient of friction with ($\mu=0.7$) has been used [12]. Sliding, which occurs when the normal stiffness (K_n) not equal zero. For most contact analysis, ANSYS estimates values for (K_n) as follows [15].

$$K_n = f \cdot E_c \cdot h \quad (6)$$

Where f = Contact compatibility factor (0.01-1.0), (FKN in ANSYS).

E_c = Concrete Young's modulus

h = Characteristic contact length

In the shear connector behavior the normal forces transmitted by the axial forces in the reinforcing bars are modeled by using a link element (LINK8 in ANSYS), while, the shear forces that are transmitted by shearing and flexure of the reinforcing bars are modeled by using a nonlinear spring element (COMBIN39 in ANSYS). The nonlinear shear stiffness (K_s) of the dowel bars is given by [13]:

4.1 MODELING OF THE BEAM

By taking advantage of the symmetry of both beam's geometry and loading, a half of the entire model beam in longitudinal direction is used for the finite element analysis. The aim of this was to reduce the computational time. The initial step of modeling involves creating key points for external points and certain locations such as support or loading and then creating lines between these key points to establish areas of steel beam and stiffeners then creating the volumes of concrete slab, anchorages and steel plates. The origin of coordinates coincides with the center of external edge of beam, as shown in Fig.4.

4.2 MESHING OF BEAM

After specifying the volumes and the areas, a F.E.analysis requires meshing of the model. In other words, the model is divided into a number of small elements, to obtain good results. After meshing the beam the tendon is modeling, the use of a rectangular mesh is recommended. The width and length of elements in the interface surface is set to be consistent elements. The mesh used is shown in Fig.5 and the number of elements is shown in Table 2.

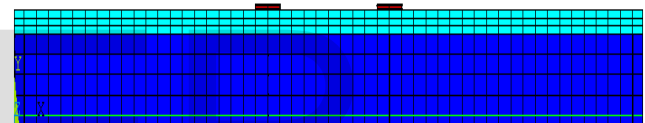
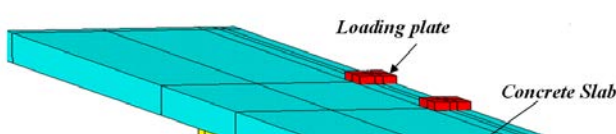


Fig. 5. Volumes and Areas of Concrete and Steel Beam in ANSYS .

TABLE 2
NUMBER OF ELEMENTS FOR TESTED BEAM

Structural Component	Number of Elements
Concrete (Slab)	2808
I-STEEL (Beam and Stiffeners)	1260
Reinforcement (Longitudinal steel, Transverse steel, Tendon ,and Steel stud)	332
Shear Connectors (Combin39)	34
Solid 45 (Loading plate and Anchorages)	112
Interface (Shear Friction and Contact)	312



4.3 INTERFACE ELEMENT MODELING

Surface-to-surface contact elements are used to model interface between concrete and top flange of the I-steel beam as shown in Fig.6.

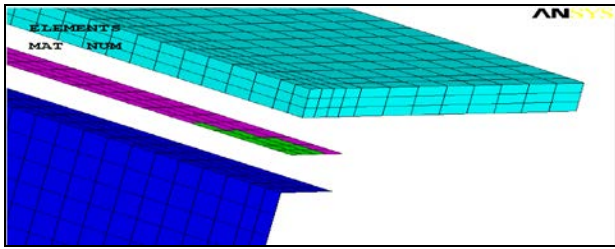


Fig. 6. Surface to Surface Contact Element.

4.4 MODELING OF SHEAR CONNECTORS

Shear connectors consisting of two types of elements, (Combine 39 and link 8) are used to model stud shear connectors between concrete and I-steel beam. Combine 39 element located between two nodes, the first node on I-steel and the second node on concrete with the same position. The second element is Link8 consist of three nodes, the first one on I-steel flange while the second and third point in concrete elements , as shown in Fig. 7.

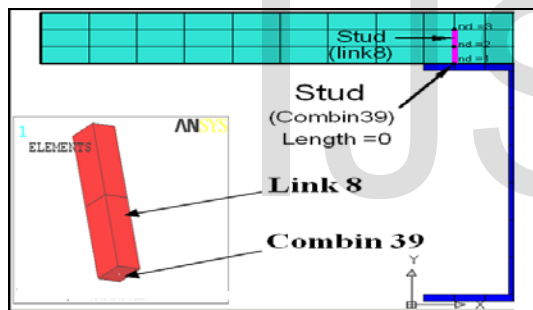


Fig. 7. Shear Connector Elements (Combine39, link8).

4.5 MODELING OF STEEL REINFORCEMENT

To model reinforcement bars, the discrete elements (LINK8) are used as shown in Figure (8). In spite of meshing of volumes for concrete beam and areas for steel section, no mesh of the reinforcement is needed because individual elements are created in the modeling through the nodes created by the mesh of the concrete volume. By advantage of discrete model, the longitudinal and transverse reinforcement are kept in their actual position.

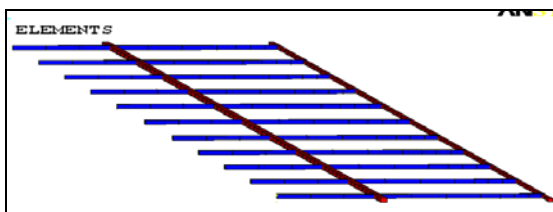


Fig. 8. Reinforcement Modeling in ANSYS for the Beam.

4.6 LOADS AND BOUNDARY CONDITION

Displacement boundary conditions are needed to constrain the model to get a unique solution. The boundary conditions need to be applied at points of symmetry and where the supports and loadings exist. Since one half of beam is taken in this model, one plane of symmetry is created. To model the symmetry, nodes on this plane must be constrained in the perpendicular direction on it, as shown in Fig.9.

The supports are modeled in such a way a hinge and roller, that the beams in the present study simply support beam. To model the roller, a single line of nodes on the support are constraint in the vertical direction ($U_y = 0$), and constrains in the vertical and longitudinal direction give as hinge support ($(U_x, U_y) = 0$).

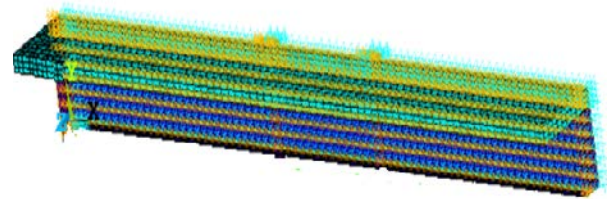


Fig. 9. Symmetry of One Half Beam.

For external loads a small bearing plate was placed between the loading and the concrete slab, to preventing concentration of stress in the concrete slab at the point of contact. Half of the loads ($P/2$) is applied because half model was used in our study, where the external load was applied by the equivalent nodal forces on the top nodes. The loads are applied on twenty nodes ten in each side.

In this study, the default of ANSYS program is used (convergence is checked by a force convergence criterion, tolerance equal to 0.001). The solution has been achieved by using the incremental-iterative techniques.

5 PARAMETRIC STUDY

The main purpose of the parametric study is to investigate the influence of some parameters such as material properties or geometric changes in structure therefore ten parameters are taken in this study

5.1 EFFECT OF COMPRESSIVE STRENGTH OF CONCRETE

To study the effect of concrete compressive strength f_c' of the concrete slab on the behavior of prestressed composite steel-concrete beam, different values of f_c' were considered. These value were (20, 30, 40, 50, and 60) MPa. Fig. 10 shows the effect of compressive strength concrete slab on the load-deflection behavior of the selected beam. The Figure indicates that the stiffness of beam increases slightly with the increase of f_c' . Also it is clear that the maximum predicated deflection is increase as the concrete compressive strength is increased.

5.2 RATIO OF EFFECTIVE PRESTRESSING STRESS TO ULTIMATE TENDON STRENGTH (F_{PE}/F_{PU})

To discuss the effect of effective prestressing stress (f_{pe}) on the behavior and ultimate load capacity of externally prestressed

composite steel-concrete beam, different values of prestressing stress have been selected. Tendons have the same ultimate strength. The chosen values for ratio (f_{pe}/f_{pu}) were (0.0, 0.25, 0.5 and 0.68). In this analysis only the value of effective prestressing stress was varied while all other parameters were kept constant. Effect of prestressing stress on the load-deflection response of the beam can be noted from Fig.11. The Figure reveals that for higher values of (f_{pe}), the ultimate load is substantially increased. This can be attributed to the effect of the external prestressing force that tends to prevent the cracks from extending and improves the stiffness.

5.3 EFFECTIVE HEIGHT OF THE EXTERNAL PRESTRESSING TENDON

The effect of the effective height of the external prestressing tendon can be taken as different values for beam VS-2 where the values chosen are (30, 75, 125, 190, and -30) mm from center of the bottom flange. The positive signs mean the tendon above the bottom flange of steel beam while the negative sign means that tendon below the bottom flange of steel beam. Typical numerical load deflection curves for different values of effective height are compared with the experimental load-deflection curve ($h_{pe} = 30$ mm) as shown in Fig.12. This Figure reveals that as a result of the decreasing effective height of externally prestressed tendon, the stiffness and ultimate load capacity are essentially increased. The predicated ultimate load is increased by average (18 %) when the tendon position change from (190 mm) to (-30 mm). This may be attributed to the increase in eccentricity of tendon which causes increase in its distance from the neutral axis, the greater the distance the higher the stress. Therefore, decreasing the tendon height to more has a significant effect on the ultimate strength capacity.

5.4 EFFECT OF EXTERNAL PRESTRESSING TECHNIQUE

This section will compare the non-prestressed composite beam results with the externally prestressed composite beam results. Fig.13 shows the curves of load against mid-span deflection for each beam. A comparison of the load-deflection curves illustrates that the prestressed beam deforms less than the non-prestressed beam, or behaves more stiffly. Both beams behaved quite linearly in the load-deflection curves before yielding of the steel bottom flange for non prestressed composite beam. The initial upward deflection had contributed to the lower deflection in the prestressed composite beam, and the tangents of the curves of prestressed composite beam are slightly greater than those of the non-prestressed beam before yielding of the steel beam, they appear quite similar. The reason should be the incremental prestress in the tendons, which is small and develops linearly with the exerted load before the yielding of the steel beam in prestressed composite beam, but increases much faster afterward. The results also demonstrate that adding prestressing to the composite beams significantly increased the yield load and the ultimate strength. It is noted the ultimate load for external prestressed composite beam is increased by 15.9 % which is larger than that of non-prestressed composite beam.

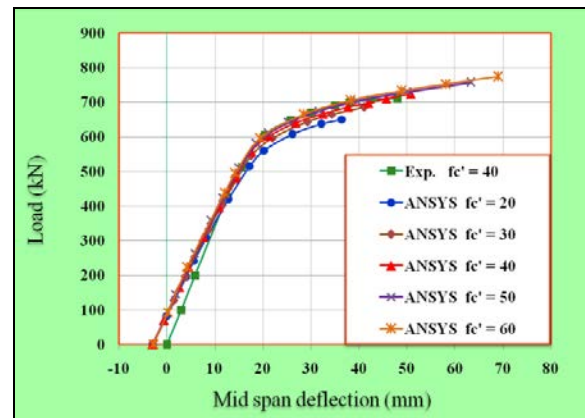


Fig.10 Effect of Compressive Strength of Concrete on the Load-Deflection Behavior of Beam Symmetry of One Half Beam.

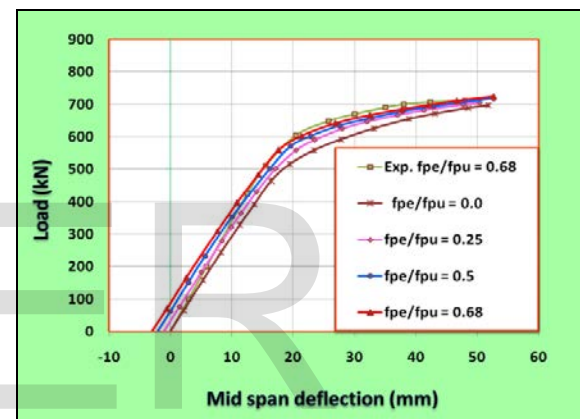


Fig.11 Effect of f_{pe}/f_{pu} Ratio on Load-Deflection Behavior of the Beam

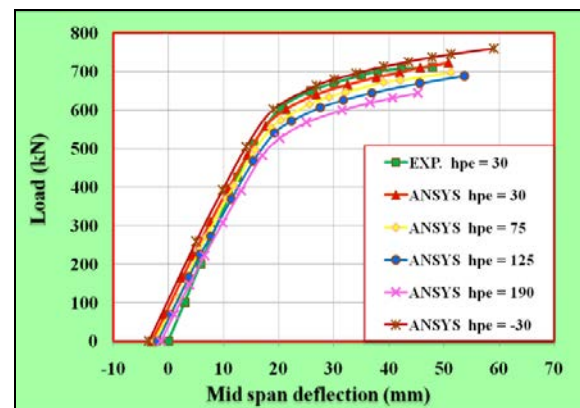


Fig.12 Effect of Effective Height of External Prestressing Tendon on Load-Deflection Behavior of Beam.

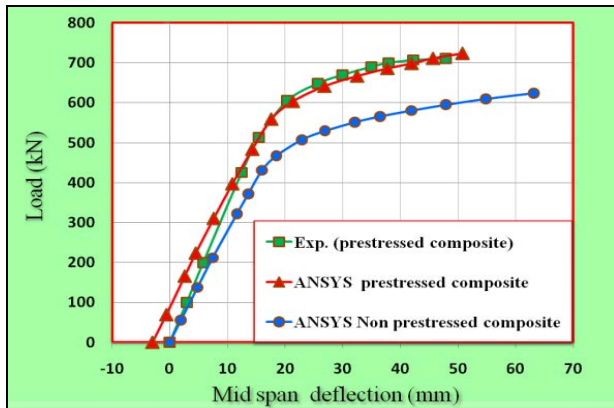


Fig.13 Load-Deflection Curves of External Prestressed Composite and non Prestressed Composite Beam.

5.5 EFFECT OF RATIO OF DEPTH (T) TO WIDTH (B) OF CONCRETE SLAB

The effect of the ratio of concrete slab depth to its width on the load-deflection behavior of prestressed composite beams and their ultimate loads are studied in this section. A different ratio of depth to width for concrete slab of VS-2 prestressed composite beam was taken in the finite element analysis. The selected ratios (t/B) were (0.086, 0.15, 0.2, and 0.25). In choosing these ratios, the total area of concrete slab was kept constant at (96300 mm²). Finite element mesh for all cases is illustrated in Fig.14. Fig.15 shows the effect of depth to width ratio on the load-deflection behavior of selected beam. In this figure, when the depth to width ratio increased, the ultimate load of has been increased distinctly. This is to be expected as an increase in thickness of slab would raise the neutral axis of the prestressed composite beam, hence increasing the eccentricity of tendon. The stiffness of beam is increased by increasing the depth to width ratio of concrete slab. Also it is clear that the maximum predicated deflection is decrease as the depth to width ratio of concrete slab is increased.

5.6 FULL AND PARTIAL INTERACTION

The present section focuses on the behavior of prestressed composite beam with full and partial interaction using the finite element software ANSYS. The results of the analysis of prestressed composite beams with full and partial interaction are presented in order to highlight the geometric nonlinear effects and how the ultimate loads are influenced by this effect. For beam with full interaction analysis is found no slip between concrete slab and steel beam is occur while for the same beam with partial interaction (1.43) mm slip was recorded at interface surface as shown in Fig.16. The finite element results obtained for the same beam assuming full and partial shear interaction are shown in Fig.17. It can be noted, that compared to a composite beam with partial shear interaction a stiffer behavior has been noticed. The ultimate load of the composite beam with full shear interaction was (764.3kN). The ratio of the ultimate load obtained using a complete shear interaction to the partial interaction value is (1.057).

5.7 INFLUENCE OF TENDON PROFILE

In this section two cases of external tendon profile are chosen to discuss the effect of tendon profile on the load - deflection response for externally prestressed composite steel-concrete beam, straight profile in first case and two draped tendon profile with in second case. Fig.18 shows the results of load-deflection response for two cases. It can be seen in this Figure that the ultimate load capacity increases with draped tendon profiles compared to undraped profiles (straight tendon profile) where is produced the lowest nominal resistance. While no change in stiffness before yielding. After yield point the draped tendon will be stiffer than straight tendon.

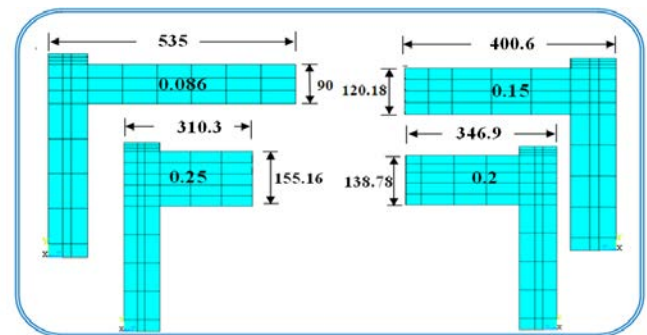


Fig.14 Finite Element Mesh for the Beam) with Different Depth to Width Ratio of Concrete Slab.

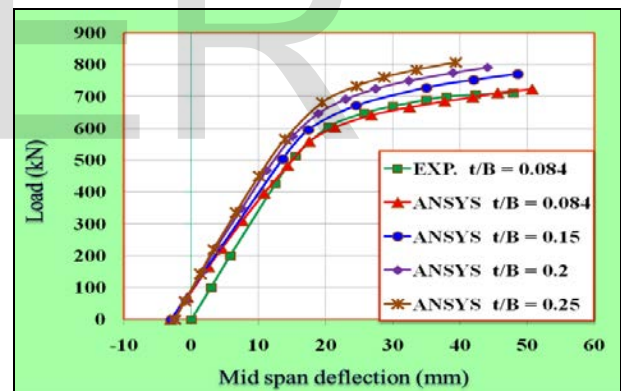


Fig.15 Effect of Effective Height of External Prestressing Tendon on Load-Deflection Behavior of Beam.

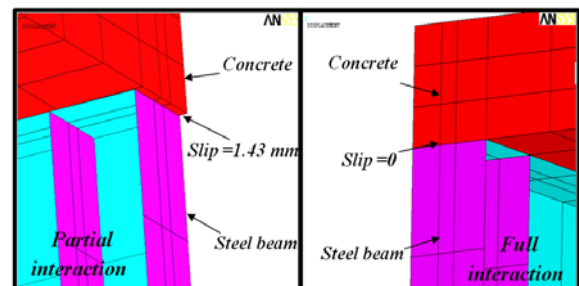


Fig.16 Numerical Relative Slip between Concrete and Steel for the Beam for Full and Partial Interaction

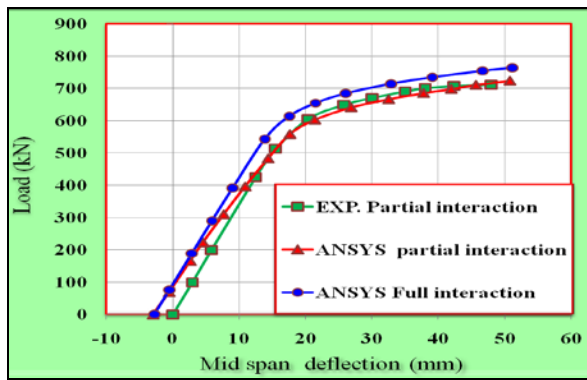


Fig.17 Effect of Degree of Interaction on the Load-Deflection Behavior of beam.

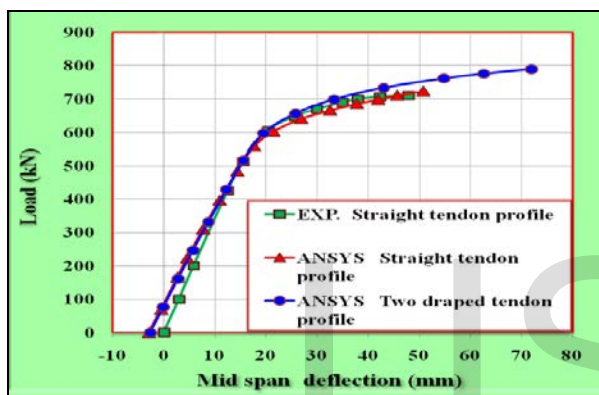


Fig.18 Effect of Tendon Profile on Load-Deflection Behavior of the Beam.

5.8 TYPES OF LOADING

The effect of load application on the load- deflection response was evaluated using three types of loading, namely, single concentrated load, two concentrated loads and four concentrated loads. Results are shown in Fig.19 these results were obtained using straight tendon profile. The increasing of load on the beam subjected to four point loads is 45 % greater than that in beam with a single load at mid span. This is because, during loading, cracks started to appear and spread as the load increased. This continued up to formation of the plastic hinge where the strain concentrated and stress increased up to failure.

5.9 EFFECT OF USING UNSYMMETRICAL I-STEEL BEAM

The effect of using unsymmetrical cross-section of steel beam on the load-deflection response of prestressed composite steel-concrete beams and their ultimate load are investigated in this section. The results are obtained by increasing the width of the lower flange of the steel beam to make its area as (A_1) and decreasing the width of the upper flange of steel beam by the same amount to make its area as (A_2). In this procedure the total area of steel beam cross-section was kept constant. Different ratios of upper flange area to lower flange area (A_1/A_2)

of the beam were taken in the numerical analyses. These ratios were (2.5, 1.6, 1.25 and 1.0), as shown in Fig.20. Fig.21 shows the effect of the upper to lower steel flange ratio on load-deflection response of prestressed composite steel-concrete beam. The overall behavior obtained from these tests ranges from stiff response when ratio (A_1/A_2) was set equal to (2.5) to a relatively soft response for (A_1/A_2) ratio equals to (1.0). Also, it has been observed that higher values of the ratio (A_1/A_2) lead to an increase in the ultimate moment capacity.

5.10 EFFECT OF NUMBER OF STIFFENERS

In order to study the influence of stiffeners on the response of externally prestressed composite steel-concrete beams, different stiffener numbers is investigated for the beam, where the selected beam is used four pairs of stiffeners two under load and two at supports. The numbers were selected to study this effect are without stiffeners , two pairs of stiffeners , four pairs of stiffeners and six pairs of stiffeners. All beams were subjected to two concentrated loads. Comparison between the four types of beam on the behavior of load-deflection response is given in Fig.22. The load deflection curves indicate no differences in behavior before yielding. While noted slightly difference in stiffness for beams after yield load.

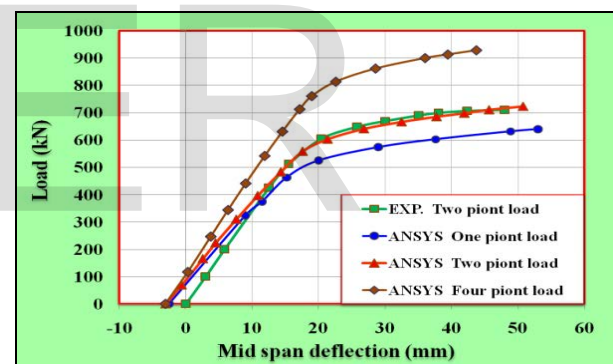


Fig. 19 Effect Type of Loading on Load -Deflection Behavior of the Beam

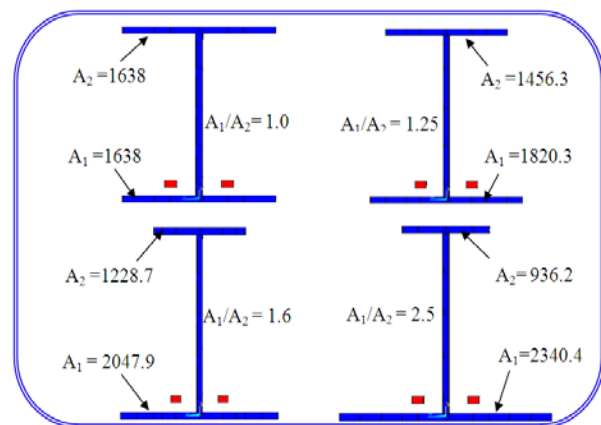


Fig.20 Finite Element Mesh for the Beam with Different Lower to Upper Steel Flange Area Ratio. (all area in mm²)

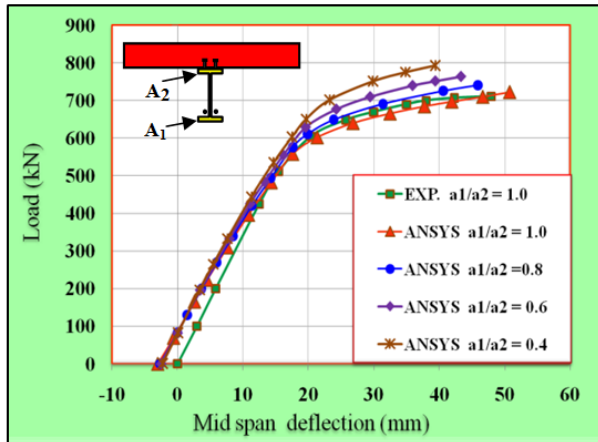


Fig.21 Effect of Ratio Upper Flange Area to Lower Flange Area on the Load-Deflection Behavior for the Beam..

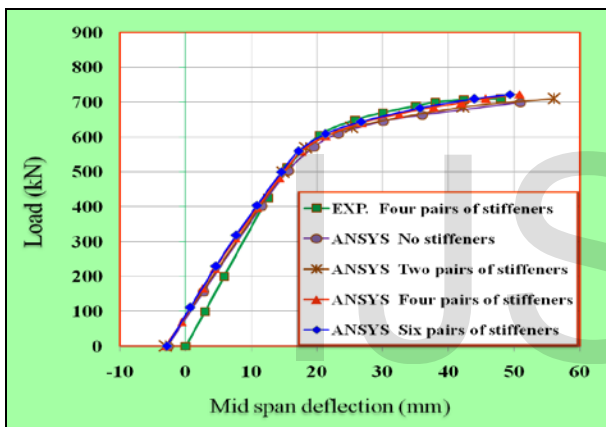


Fig.22 Effect of Number of Stiffeners on Load-Deflection Curve of the Beam.

6 CONCLUSIONS

A numerical nonlinear analysis model, based on the Finite Element Method (FEM) using ANSYS computer program, was developed to investigate the effect of several factors on load-deflection response throughout the entire range of behavior using the nonlinear analysis by ANSYS computer program. Effect of these factors can be summarized as follows:

- 1- From the numerical analysis carried out to study the effect of compressive strength of concrete on the strength behavior, it was found that as the compressive strength of concrete is increased from 20 N/mm² to 60 N/mm² the ultimate load is increased by about 18.9 %.
- 2- For different values of effective prestressing stress that are taken as f_{pe}/f_{pu} ratio, the ultimate load is increased substantially by about 3.74 % when the ratio is increased from 0.0 to 0.68. This can be attributed to increase in prestressing force that improves the stiffness of beam.

3- It was found from the numerical analysis that the predicted ultimate loads are increased by 18% when the tendon position change from (190 mm) to (-30 mm).

4- It was observed that the increase in the ultimate load capacity for external prestressed beam by 15.9 % is larger than the same beam without external tendon.

5- The strength of composite beams are increased by increasing the ratio of the depth to width of concrete slab (t/B), with keeping the total area of concrete slab constant and it was found that as the (t/B) ratio is increased from 0.084 to 0.25 the ultimate load increases by about 11.68 %.

6- The finite element results obtained for the same beam assuming full and partial shear interactions are shown that compared to a composite beam with partial shear interaction a stiffer behavior has been noticed. It was observed that the ultimate load capacity for beam with full interaction increase by 5.71 % is larger than the same beam with partial interaction.

7- It was found that the tendon profile has a clear effect on the ultimate load capacity. The ultimate load increased 9.23 % with two draped tendon profile compared to undraped profile.

8- The increased in ultimate load on the beam subjected to four point loads is 45 % greater than that in beam with a single load at mid span.

9- It was found that the unsymmetrical I-section steel beam with wider bottom flange used in prestressed composite steel-concrete beam is more effective without change of total cross section area. It was noticed that when the ratio of top flange area to bottom flange area for I-section steel beam (A_1/A_2) is increased from 1.0 to 2.5, the ultimate load increased by about 9.7 %.

10- Stiffeners web plate has no significantly effect on the behavior of prestressed composite steel-concrete beams, where the results showed that when increased number of stiffeners to six pairs of stiffeners the ultimate load increased by about 3.3% . Beam with stiffeners and without stiffeners exhibit a very similar load - deflection response.

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